

Macroeconomic Theory 102  
Winter 2015 - François Geerolf  
Midterm 2  
Wednesday, February 25, 2015  
Time Limit: 75 Minutes

Last Name: \_\_\_\_\_

First Name: \_\_\_\_\_

Teaching Assistant: \_\_\_\_\_

Student ID Number: \_\_\_\_\_

Signature \_\_\_\_\_

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## Test A

This exam contains 11 pages (including this cover page). You can earn 100 points.

### Instructions:

1. Print your Last name, First Name, Teaching Assistant Name (as a reminder, teaching assistants are: Flavien Moreau, Keyyong Park, Matias Vieyra, and Gabriel Zaourak), Student ID Number and Signature at the top of this page.
2. The only items which should be on your desk are pencils and/or pens. NO other items are allowed. Place any other item UNDER your desk. Calculators are NOT allowed.
3. Once the exam begins, you are not allowed to leave the room until you hand in your exam.

**Good luck ! Budget your time wisely ! (skip the question or even the exercise if you get stuck)**

Grade Table (FOR TEACHER USE ONLY)

Question	Points	Score
1	30	
2	15	
3	5	
4	50	
Total:	100	

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## Multiple Choice (30 points)

1. (30 points) Mark box if true - each multiple choice question has only one right answer.
  - (a) (2 points) If  $P_t$  is the price level in time  $t$ , then inflation is calculated as:
    - $1/P_t$
    - $P_{t+1}/P_t$
    - $P_{t+1} - P_t$
    - $P_t/P_{t+1}$
    - $(P_{t+1} - P_t)/P_t$
  - (b) (2 points) In the United States, money is backed by:
    - oil
    - gold
    - silver
    - no physical commodity
    - None of these answers are correct.
  - (c) (2 points) According to the quantity theory of money, the price level is:
    - Exogenous
    - Determined by the money supply only
    - Determined by the ratio of the effective quantity of money to the volume of goods
    - Indeterminate in the long run
    - Determined by the volume of goods produced
  - (d) (2 points) Net worth is equal to a bank's
    - investments minus deposits
    - cash plus reserves
    - deposits plus loans
    - loans minus capital
    - total assets minus total liabilities
  - (e) (2 points) Using the IS curve  $\tilde{Y}_t = \bar{a} - \bar{b}(R_t - \bar{r})$ , in the long run,  $\bar{a}$  \_\_\_\_\_ and \_\_\_\_\_, so that \_\_\_\_\_.
    - equals one;  $R_t = \bar{r}$ ; the economy is in recession
    - is greater than one;  $R_t > \bar{r}$ ; the economy is at its long-run equilibrium
    - equals zero;  $R_t = \bar{r}$ ; the economy is at its long-run equilibrium
    - equals one;  $\bar{b} = \bar{a}$ ; the economy is expanding
    - equals one;  $R_t = 1$ ; the economy is in recession.
  - (f) (2 points) Consider the consumption function  $C_t/\bar{Y}_t = \bar{a}_c + \bar{x}\tilde{Y}_t$ . If  $\bar{x} = 0.5$ , a 2 percent demand shock:

- raises short-run output by 1 percent  
 raises short-run output by 0.5 percent  
 raises short-run output by 4 percent  
 reduces short-run output by 4 percent  
 has no impact on short-run output
- (g) (2 points) With adaptive expectations, the Phillips curve can be written as:
- $\Delta\pi_t = \bar{\nu}\tilde{Y}_t$   
  $\Delta\pi_t = \pi_{t-1} + \bar{n}\bar{u}\tilde{Y}_t$   
  $\pi_t = \pi_{t+1} + \bar{\nu}\tilde{Y}_t$   
  $\Delta\pi_t = \bar{\nu}u_t$   
  $\pi_t = \pi_{t-1}$
- (h) (2 points) Which of the following best describes why the aggregate demand curve slopes downward ?
- If the central bank observes a low rate of inflation, the monetary policy rule dictates an increase in the real interest rate. The high interest rate reduces output by reducing investment demand in the economy.  
 If the central bank observes a high rate of inflation, the monetary policy rule dictates a decrease in the real interest rate. The low interest rate increases output by reducing investment demand in the economy.  
 If the central bank observes a high rate of inflation, the monetary policy rule dictates an increase in the real interest rate. The high interest rate reduced output by reducing investment demand in the economy.  
 If the central bank observes a low rate of inflation, the monetary policy rule dictates a decrease in the real interest rate. The low interest rate reduces output by reducing investment demand in the economy.  
 None of these answers is correct.
- (i) (2 points) The adjustment process back to the steady state in the short-run model hinges on the:
- rate of unemployment  
 immediate reaction to a change in the inflation rate  
 consumers' response to inflation shocks  
 government's response to inflation shocks  
 slow adjustment of inflation reflected in the aggregate supply curve.
- (j) (2 points) Which of the following represents the AD curve with a financial friction?
- $\tilde{Y}_t = \bar{a} - \bar{b}\bar{f} - \bar{b}\bar{m}(\pi_t - \bar{\pi})$ .  
  $\tilde{Y}_t = \bar{a}(1 + \bar{b}\bar{f}) - \bar{b}\bar{m}(\pi_t - \bar{\pi})$ .  
  $\tilde{Y}_t = \frac{\bar{a}}{\bar{b}\bar{f}} - \bar{b}\bar{m}(\pi_t - \bar{\pi})$   
  $\tilde{Y}_t = \bar{a} - \bar{m}\bar{f} - \bar{b}\bar{m}(\pi_t - \bar{\pi})$ .

$\tilde{Y}_t = \bar{a} - \bar{f} - \bar{b}\bar{m}(\pi_t - \bar{\pi}).$

(k) (2 points) The Fisher equation is given by:

$u_t - \bar{u} = -(1/2)\tilde{Y}_t$

$\bar{P}_t^* = \frac{M_t \bar{V}}{Y_t}.$

$\Delta\pi_t = \bar{\nu}\tilde{Y}_t + \bar{o}$

$i_t = R_t - \pi_t.$

$i_t = R_t + \pi_t.$

(l) (2 points) When the central bank announces expansionary monetary policy and all other economic agents build this into their decision making, as a consequence \_\_\_\_\_ with no economic benefit; this is called the \_\_\_\_\_ problem.

output rises; policy lag

unemployment rises; time inconsistency

expectations rise; adaptive expectations

inflation rises; time inconsistency

inflation rises; discretionary

(m) (2 points) In the presence of rational expectations, the central banks' willingness to battle inflation:

causes future inflation

becomes a determinant of past inflation

undermines the ability to fight inflation

becomes a determinant of expected inflation

weakens the central government.

(n) (2 points) If the government gives firms a temporary investment tax credit:

firms will invest now rather than in the future

it will increase  $\bar{a}_i$

it will increase  $\bar{a}$

All of these answers are correct

None of these answers are correct

(o) (2 points) Suppose we assume that initially  $\bar{a} = 0$ ,  $\bar{b} = 0.5$ ,  $R_t = \bar{r} = 5\%$ ; if  $\bar{a}_c$  rises 2 percent and the real interest rate falls 2 percent, short-run output:

falls 2 percent

rises 1 percent

rises 3 percent

falls 1 percent

does not change

## Exercise 1 (15 points)

2. (15 points) Consider the following balance sheets for three hypothetical financial institutions, bank A, bank B and bank C.

### Bank A's Balance Sheet

Assets		Liabilities	
Cash	600	Deposits	1400
Loan to bank B	500		
Mortgage-Backed Securities	400		
Total assets	—	Total Liabilities	—
		Equity (net worth)	—

### Bank B's Balance Sheet

Assets		Liabilities	
Cash	1000	Deposits	900
Loan to bank C	500	Loan from Bank A	500
Total assets	—	Total Liabilities	—
		Equity (net worth)	—

### Bank C's Balance Sheet

Mortgage-Backed Securities	800	Deposits	200
		Loan from Bank B	500
Total assets	—	Total liabilities	—
		Equity (net worth)	—

- (a) (2.5 points) Fill in the missing entries in the balance sheets (denoted —).
- (b) (2.5 points) What is the leverage ratio in each bank?

- (c) (10 points) Suppose housing prices fall sharply and the mortgage-backed securities as a consequence fall in value by 50%. Assume that banks first make good on their deposits, before actually repaying other banks. Calculate bank A's new net worth. (be careful, two banks hold Mortgage-Backed Securities !)

**Exercise 2 (5 points)**

3. (5 points) According to the life-cycle/ permanent-income hypothesis, consumption depends on the present discounted value of income. An increase in the real interest rate will make future income worth less, thereby reducing the present discounted value and reducing consumption. To incorporate this channel into the model, suppose the consumption equation is given by:

$$C_t = \bar{a}_c \bar{Y}_t - \bar{b}_c (R_t - \bar{r}) \bar{Y}_t.$$

Derive the IS curve for this new specification.

### Exercise 3 (50 points)

4. (50 points) Take the usual AS/AD model, ruling out Aggregate Demand shocks, so with  $\bar{a} = 0$ , but assuming a one-time, unexpected oil price shock  $\bar{o}_0 > 0$ . One time means that the oil price shock lasts only for one period, in period  $t = 0$ , and that  $\bar{o}_t = 0$  for all subsequent  $t \in \{1, 2, \dots\}$ . Unexpected means that the economy was originally in steady-state, and in particular that  $\pi_0 = \bar{\pi}$ . Unless otherwise noted, agents have adaptive expectations about inflation. The economy is described by an AS/AD model. In particular, the AS curve is given by (be careful about the convention on the timing of the oil shock  $\bar{o}_{t-1}$  !):

$$\pi_t = \pi_t^e + \bar{\nu}\tilde{Y}_t + \bar{o}_{t-1}.$$

The AD curve is the standard one used throughout the course.

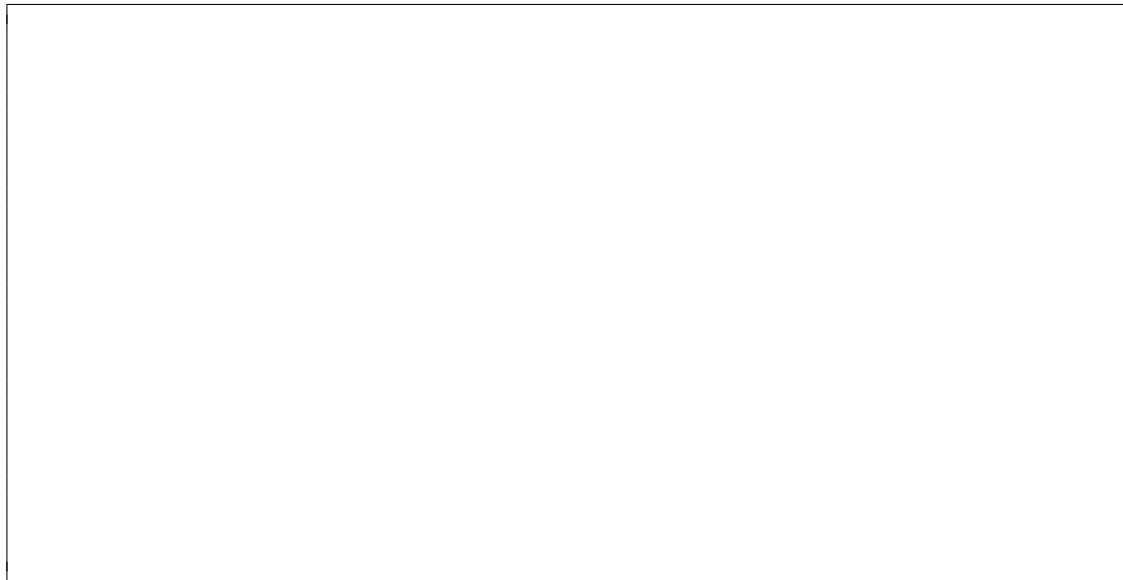
- (a) (5 points) What are the values of  $\pi_1$  and  $\tilde{Y}_1$  in terms of the parameters of the model? (in particular the size of the oil price shock,  $\bar{o}_0$ )

- (b) (5 points) Show analytically<sup>1</sup> the effect of a more aggressive monetary policy on inflation and short-run output in period 1: do inflation and short-run output increase or decrease with a more aggressive monetary policy?

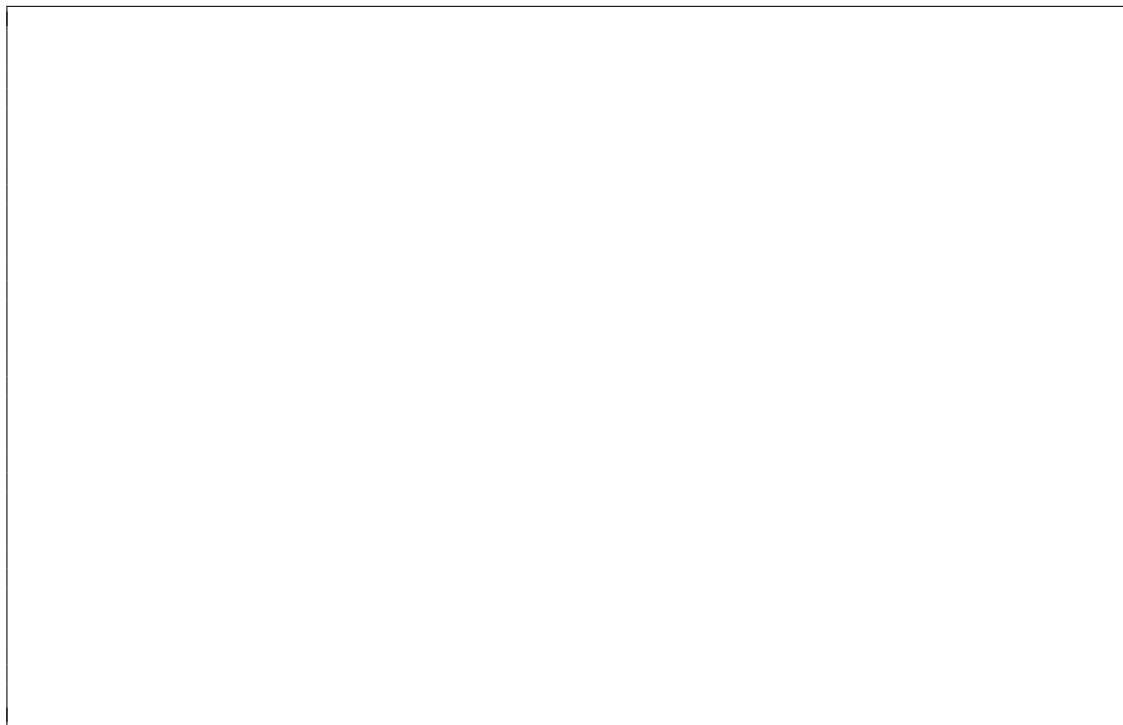
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<sup>1</sup>That is, in mathematical terms.

- (c) (5 points) Illustrate this on two graphs with the AS/AD curves: show one AS/AD diagram with a soft monetary policy, and next to it another AS/AD diagram with an aggressive monetary policy. Show  $\pi_1$  and  $\tilde{Y}_1$  as well as the long run values of inflation and short-run output on these graphs.



- (d) (5 points) Eliminating  $\tilde{Y}_t$  from the AS/AD model, find a difference equation<sup>2</sup> for  $\pi_t$ , for  $t \in \{2, 3, \dots\}$ .



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<sup>2</sup>A difference equation is an expression of an economic quantity as a function of its previous (lagged) values, generally the value in the previous period. For example  $\pi_t$  expressed as a function of  $\pi_{t-1}$  is a difference equation for  $\pi_t$



- (e) (5 points) Subtracting  $\bar{\pi}$  on both sides in the difference equation for  $\pi_t$ , show that  $\pi_t - \bar{\pi}$  satisfies a simpler difference equation than  $\pi_t$ .<sup>3</sup> Solve for this difference equation. This should give you an expression for  $\pi_t$  as a function of  $\pi_1$ . Then replace  $\pi_1$  with the value found in question (a), to get  $\pi_t$  as a function of time and the parameters of the model.

- (f) (5 points) Use the (AD) curve to then calculate  $\tilde{Y}_t$  as a function of time and the parameters of the model.

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<sup>3</sup>Simpler in the sense that you can solve for it. For example, a simple difference equation is one of the form  $u_t = \rho u_{t-1}$ , whose solution is  $u_t = \rho^{t-1} u_1$ .

- (g) (5 points) Numerical Application: Suppose the parameters of the AS and AD curves take the following values:  $\bar{o}_0 = 2\%$ ,  $\bar{a} = 0$ ,  $\bar{b} = 1/2$ ,  $\bar{m} = 1/2$ ,  $\bar{v} = 1/2$ , and  $\bar{\pi} = 2\%$ . Solve for the value of short-run output and the inflation rate for the first 2 years after the shock. (express your result as a single fraction, since you do not have a calculator !)

- (h) (5 points) Calculate how much realized inflation differs from expected inflation, or  $\pi_t - \pi_t^e$ , for any  $t \geq 1$ , in this model. Simplify the expression so that its sign appears clearly.<sup>4</sup>

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<sup>4</sup>That is, it should be clear from your expression of  $\pi_t - \pi_t^e$  whether it is positive or negative

- (i) (5 points) Why are these adaptive expectations where  $\pi_t^e = \pi_{t-1}$  considered as "non rational" ? What is irrational about them?

- (j) (5 points) What would  $\pi_t - \pi_t^e$  be equal to under rational expectations?